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MATERIALS FOR THE STUDY OF DEEP-FOCUS EARTHQUAKES* (SECOND PAPER)

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INTRODUCTION

THE PRESENT PAPER is supplementary to a previous publication under the same title,¹ for which a list of errata is here given.² The first paper has been translated into French by Professor E. Rothé, and is to be published by the Bureau Central Séismologique International. (The French publication will contain a travel-time chart for focal depth 600 km. in place of that for 400 km. given in the English paper.) At the request of Professor Rothé a more detailed account of the calculation of certain travel times was drawn up, which he has also translated, and which will appear as an additional note in the French publication. This additional note is given in English in the present paper. To this are added a new table (table 1, pp. 161-165 below) giving epicentral distance as a function of the travel time of P and of the focal depth, and a further discussion of methods for locating the epicenters of deep shocks.

CALCULATION OF TIMES FOR pP, sS, sP, pS

In figure 1 let G be the hypocenter of a shock at depth A for which the travel times of P and S are known; in particular, this may be a normal shock, with A assumed as 25 km. Let H be another hypocenter at depth B (which may be 100, 200, 300 . . . km.), and consider a ray passing through both G and H. For the hypocenter H the time along this ray to a distant station will be decreased by

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¹ B. Gutenberg and C. F. Richter, "Materials for the Study of Deep-Focus Earthquakes," *Bull. Seism. Soc. Am.*, 26:341-390 (1936).

² Errata in the previous paper:

- P. 351, table 8, 70°, 700 km., for 11:26 read 12:26.
- P. 361, table 22, 105°, 300 km., for 37:21 read 27:21.
- P. 368, table 36, 65° and 70°; all six minutes given as 48 should read 47.
- P. 370, table 40, 65°, 500 km., for 19:47 read 18:47.
- P. 377, table 46, heading, read $0 = (pP + P)/2 - t_p - c$.
- P. 377, table 46, 80°, 700 km., for 5 read 4.
- P. 379, table 48, 2:15, 90°, for 603 read 630.
- P. 383, table 51, Bombay, minute of S; for 8 read 7.
- P. 383, table 51, Manila, minute of S; for 14 read 15.
- P. 384, table 51, column heading; for 36^d 10^h 38^m read 836^d 10^h 38^m.

the time along GH, while the distance will be decreased by DE (D, E being the epicenters corresponding to G, H). The time from G to H is $\int_A^B \frac{dr}{v \cos i}$, and DE is $\int_A^B \frac{\tan i}{r} dr$. That is, if for the depth A we have travel-time t at distance Δ , then for depth B we have time $t - \int_A^B \frac{dr}{v \cos i}$ at distance $\Delta - \int_A^B \frac{\tan i}{r} dr$. By varying the assumptions (initial angle of incidence; or, better, the initial epicentral dis-

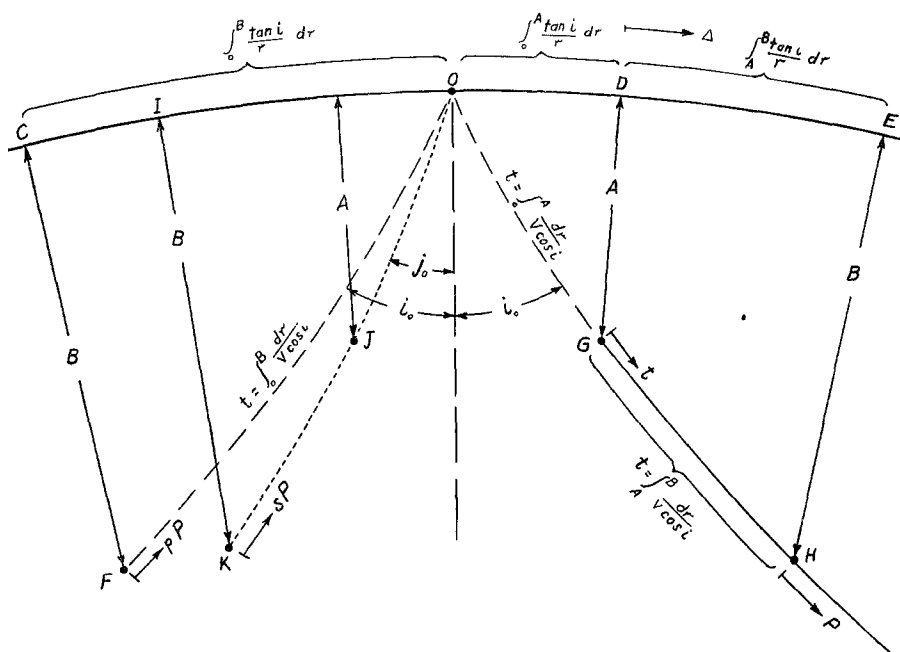


Fig. 1.

tance at G) the whole curve for depth B can be constructed without the necessity of any approximation.

The figure shows that the times for pP may be derived by a similar process. If the hypocenter F is at depth B , the path of pP is FOGH, so that the travel time of pP originating at F is equal to that of P originating at G plus the times along FO and OG; and the corresponding distance is that of G increased by CO and OD. The time along FO + OG is $\int_0^B \frac{dr}{v \cos i} + \int_0^A \frac{dr}{v \cos i}$, and CO + OD =

$\int_0^B \frac{\tan i}{r} dr + \int_0^A \frac{\tan i}{r} dr$. Hence if for depth A we have the travel time of P at distance Δ , then at depth B we have the travel time for pP

$$t + \int_0^B \frac{dr}{v \cos i} + \int_0^A \frac{dr}{v \cos i} \text{ at distance } \Delta + \int_0^B \frac{\tan i}{r} dr + \int_0^A \frac{\tan i}{r} dr.$$

This is the result stated in the first paper, and again no approximation is involved.

The procedure for S and sS is exactly analogous to that for P and pP. For sP and pS it is more complicated, and is best explained in connection with a particular example.

Suppose that we wish to derive times for a focal depth of 300 km. from those for a normal shock at $\Delta = 45^\circ$. Table 5 of "On Seismic Waves I"³ gives the travel time of P in this case as 8^m 20^s. The corresponding time for S is given in table 19, "On Seismic Waves, II," as 14^m 54^s. The quantity $\frac{1}{\bar{v}_{40}}$ is .0726 for P and 0.127 for S (tables 16 and 20, "On Seismic Waves, II").

The corrections to time and distance required to pass to the case of 300-km. focal depth are taken from tables 1, 2, 3, and 4 of the first paper (1936). The results are:

	Distance (degrees)	Time (min.:sec.)
P for normal shock.....	45.0	8:20
Correction GH (tables 1a, 2a).....	-1.9	-0:43
P for depth 300 km.....	43.1	7:37
P for normal shock.....	45.0	8:20
Correction GOF (tables 1b, 2b).....	2.1	0:52
pP for depth 300 km.....	47.1	9:12
S for normal shock.....	45.0	14:54
Correction GH (tables 3a, 4a).....	-1.8	-1:15
S for depth 300 km.....	43.2	13:39
S for normal shock.....	45.0	14:54
Correction GOF (tables 3b, 4b).....	2.1	1:32
sS for depth 300 km.....	47.1	16:26

³ B. Gutenberg and C. F. Richter, "On Seismic Waves," *Gerlands Beitr. z. Geophys.*, 43:56-133 (1934); second paper, *ibid.*, 45:280-360 (1935).

To derive times for sP, consider the hypocenter K at depth B . The wave is transverse on the path KO and longitudinal on the path OG. Take a point J at depth A on KO. Let w be the velocity of transverse waves, v that of longitudinal waves; w_0 and v_0 are their values at the surface, \bar{w} and \bar{v} are apparent velocities. Let j_0 be the angle of incidence of the ray KO at the surface, i_0 being that of OG. Then $\frac{\sin j_0}{\sin i_0} = \frac{w_0}{v_0}$. At any depth along a given ray $\bar{v} = \frac{v_0}{\sin i_0}$, $\bar{w} = \frac{w_0}{\sin j_0}$.

Hence \bar{w} for KO equals \bar{v} for OG.

It follows that in computing for sP we use throughout the apparent velocity of the longitudinal ray through G and H, and for pS we use that of the corresponding transverse ray; in our example these are the reciprocals of 0.0726 and 0.127, respectively. For sP

	Distance (degrees)	Time (min.: sec.)
P for normal shock.	45.0	8:20
Correction GO (tables 1a, 2a, h=0)	0.1	0:05
Correction OJ (tables 3a, 4a, h=0)	0.1	0:07
Correction JK (tables 3a, 4a, h=300)	0.8	1:05
sP for depth 300 km.	46.0	9:37

If with these data we try to calculate a corresponding point for pS, we find that in tables 1 and 2 (of the first paper: 1936), which should give the last two corrections, there is no entry for the required reciprocal apparent velocity, 0.127. pS does not exist for the given distance and depth. (Cf. table 16.)

An example for pS may be obtained by calculation for a distance of 90° and focal depth 300 km. We have $\frac{1}{v_{40}} = 0.091$.

	Distance (degrees)	Time (min.: sec.)
S for normal shock.	90.0	23:54
Correction, tables 3a, 4a, h=0	0.1	0:08
Correction, tables 1a, 2a, h=0	0.1	0:05
Correction, tables 1a, 2a, h=300	3.0	0:52
pS for depth 300 km.	93.2	24:59

Individual results obtained by such calculation will often differ by a few seconds from those tabulated in the paper, which are based on smoothed curves corresponding to tables 1 to 4 (1936) and have then been subjected to further smoothing by means of table 5 (1936).

TABLE 1
EPICENTRAL DISTANCES FOR GIVEN TRAVEL TIMES OF P AND GIVEN FOCAL DEPTH

P-O (min.: sec.)	Focal depth in km.								
	25	100	200	300	400	500	600	700	800
0:30	1.7	2.0	0.9						
35	2.0	2.4	1.7						
40	2.4	2.7	2.2	0.6					
45	2.8	3.1	2.6	1.7					
50	3.1	3.5	3.0	2.4	0.0				
55	3.5	3.9	3.4	2.9	1.7				
1:00	3.8	4.3	3.8	3.4	2.7				
05	4.1	4.7	4.2	3.8	3.3	1.9			
10	4.5	5.1	4.6	4.3	3.8	2.9			
15	4.8	5.4	5.0	4.7	4.3	3.7	2.0		
20	5.2	5.8	5.4	5.1	4.9	4.4	3.1	0.0	
25	5.6	6.0	5.8	5.6	5.4	5.1	4.0	2.2	
30	5.9	6.3	6.2	6.0	5.9	5.6	4.8	3.5	1.1
35	6.3	6.7	6.6	6.5	6.4	6.1	5.4	4.4	3.0
40	6.6	7.0	7.0	6.9	6.8	6.6	6.0	5.0	4.0
45	7.0	7.3	7.4	7.3	7.3	7.1	6.5	5.7	4.8
50	7.3	7.7	7.8	7.7	7.7	7.6	7.0	6.3	5.6
55	7.7	8.1	8.1	8.1	8.2	8.1	7.5	7.0	6.3
2:00	8.1	8.5	8.5	8.5	8.7	8.6	8.1	7.6	7.0
05	8.4	8.8	8.9	8.9	9.1	9.1	8.6	8.2	7.8
10	8.7	9.2	9.3	9.4	9.5	9.5	9.2	8.8	8.5
15	9.1	9.6	9.6	9.8	9.9	9.9	9.7	9.4	9.1
20	9.5	9.9	10.0	10.2	10.3	10.3	10.2	10.0	9.8
25	9.9	10.3	10.4	10.6	10.7	10.8	10.7	10.6	10.4
30	10.2	10.6	10.7	11.0	11.1	11.2	11.2	11.2	11.0
35	10.6	11.0	11.1	11.4	11.6	11.7	11.7	11.7	11.5
40	10.9	11.4	11.5	11.8	12.1	12.2	12.2	12.2	12.0
45	11.2	11.7	11.9	12.2	12.5	12.7	12.7	12.7	12.6
50	11.6	12.0	12.3	12.6	12.9	13.1	13.2	13.2	13.1
55	12.0	12.4	12.7	13.0	13.4	13.6	13.7	13.7	13.6
3:00	12.3	12.8	13.1	13.4	13.8	14.0	14.1	14.2	14.1
05	12.7	13.2	13.5	13.8	14.2	14.4	14.5	14.7	14.6
10	13.1	13.6	13.8	14.2	14.6	14.9	15.0	15.2	15.1
15	13.4	13.9	14.2	14.5	15.1	15.4	15.5	15.7	15.6

TABLE 1—(Continued)

P-O (min.: sec.)	Focal depth in km.								
	25	100	200	300	400	500	600	700	800
3:20	13.8	14.3	14.6	15.0	15.5	15.8	15.9	16.2	16.2
25	14.2	14.6	15.0	15.4	16.0	16.3	16.5	16.7	16.8
30	14.6	15.0	15.4	15.8	16.4	16.7	17.0	17.2	17.2
35	15.0	15.4	15.8	16.2	16.8	17.2	17.5	17.8	18.0
40	15.3	15.8	16.2	16.7	17.3	17.7	18.1	18.3	18.6
45	15.7	16.2	16.6	17.1	17.7	18.2	18.6	18.9	19.1
50	16.1	16.6	17.1	17.6	18.2	18.7	19.2	19.5	19.7
55	16.5	17.0	17.5	18.1	18.7	19.2	19.7	20.0	20.3
4:00	16.9	17.4	18.0	18.6	19.2	19.7	20.2	20.6	20.9
05	17.3	17.8	18.5	19.1	19.7	20.2	20.7	21.1	21.4
10	17.8	18.3	19.0	19.6	20.2	20.8	21.3	21.7	22.0
15	18.2	18.8	19.4	20.0	20.7	21.3	21.9	22.2	22.5
20	18.6	19.2	19.8	20.5	21.2	21.8	22.4	22.8	23.1
25	19.1	19.6	20.3	21.0	21.7	22.3	22.9	23.4	23.7
30	19.5	20.0	20.8	21.5	22.2	22.8	23.5	24.0	24.3
35	20.0	20.5	21.3	22.1	22.8	23.4	24.1	24.5	24.9
40	20.5	21.0	21.8	22.6	23.4	24.0	24.7	25.1	25.5
45	20.9	21.4	22.2	23.1	24.0	24.6	25.3	25.7	26.1
50	21.4	21.9	22.7	23.6	24.5	25.2	25.9	26.3	26.6
55	21.8	22.5	23.3	24.2	25.1	25.9	26.4	26.9	27.2
5:00	22.3	23.0	23.8	24.7	25.6	26.5	27.1	27.5	27.8
05	22.8	23.5	24.4	25.3	26.2	27.0	27.6	28.1	28.4
10	23.3	24.0	24.9	25.9	26.8	27.6	28.2	28.7	29.0
15	23.8	24.5	25.5	26.5	27.4	28.2	28.8	29.3	29.6
20	24.3	25.0	26.0	27.1	28.0	28.8	29.4	29.9	30.2
25	24.8	25.6	26.6	27.7	28.6	29.4	30.0	30.4	30.8
30	25.3	26.1	27.2	28.3	29.2	30.0	30.6	31.0	31.3
35	25.9	26.7	27.8	28.8	29.7	30.5	31.2	31.6	31.9
40	26.4	27.2	28.3	29.4	30.3	31.1	31.7	32.1	32.5
45	27.0	27.7	28.8	29.9	30.9	31.7	32.3	32.7	33.1
50	27.5	28.2	29.4	30.5	31.5	32.3	32.9	33.3	33.7
55	28.1	28.8	29.9	31.0	32.1	32.9	33.5	34.0	34.3
6:00	28.7	29.3	30.5	31.6	32.7	33.5	34.1	34.5	34.9
05	29.3	29.9	31.1	32.2	33.3	34.1	34.7	35.1	35.5
10	29.9	30.5	31.7	32.8	33.9	34.6	35.2	35.7	36.1
15	30.4	31.1	32.3	33.4	34.5	35.2	35.8	36.3	36.7

TABLE 1—(Continued)

P-O (min.: sec.)	Focal depth in km.								
	25	100	200	300	400	500	600	700	800
6:20	30.9	31.7	32.9	34.0	35.1	35.8	36.4	36.9	37.4
25	31.7	32.3	33.4	34.6	35.7	36.4	37.0	37.6	38.2
30	32.2	32.9	34.0	35.2	36.3	36.9	37.6	38.3	38.9
35	32.8	33.5	34.7	35.8	36.9	37.5	38.2	38.9	39.6
40	33.3	34.1	35.3	36.4	37.5	38.1	38.8	39.6	40.3
45	33.9	34.7	35.9	37.0	38.0	38.7	39.4	40.2	41.0
50	34.4	35.3	36.5	37.6	38.6	39.3	40.0	40.8	41.7
55	35.0	35.9	37.1	38.2	39.2	39.9	40.7	41.5	42.3
7:00	35.7	36.5	37.6	38.7	39.7	40.5	41.4	42.2	43.0
05	36.2	37.0	38.2	39.3	40.3	41.1	42.0	42.9	43.7
10	36.8	37.6	38.8	39.9	40.9	41.7	42.6	43.5	44.4
15	37.3	38.2	39.4	40.5	41.5	42.4	43.3	44.2	45.1
20	37.9	38.7	40.0	41.1	42.1	43.1	44.0	44.9	45.8
25	38.4	39.3	40.6	41.7	42.7	43.7	44.7	45.6	46.5
30	39.0	39.9	41.2	42.3	43.3	44.4	45.4	46.2	47.1
35	39.7	40.5	41.8	42.9	44.0	45.1	46.0	46.9	47.8
40	40.2	41.1	42.3	43.5	44.7	45.7	46.7	47.6	48.4
45	40.8	41.7	42.9	44.1	45.3	46.4	47.3	48.3	49.1
50	41.4	42.2	43.6	44.9	46.1	47.2	48.0	48.9	49.8
55	42.0	42.8	44.2	45.5	46.8	47.9	48.7	49.6	50.5
8:00	42.6	43.5	44.9	46.2	47.4	48.5	49.4	50.3	51.2
05	43.1	44.2	45.5	46.8	48.0	49.1	50.1	51.0	51.9
10	43.7	44.9	46.2	47.5	48.7	49.8	50.8	51.7	52.6
15	44.3	45.6	46.9	48.2	49.4	50.5	51.5	52.4	53.3
20	45.0	46.2	47.6	48.9	50.1	51.2	52.2	53.1	54.0
25	45.7	46.9	48.3	49.6	50.8	51.9	52.9	53.8	54.7
30	46.4	47.6	48.9	50.2	51.5	52.6	53.6	54.5	55.3
35	47.1	48.3	49.6	50.9	52.1	53.3	54.3	55.2	56.0
40	47.7	49.0	50.3	51.6	52.8	53.9	55.0	55.9	56.7
45	48.4	49.6	50.9	52.2	53.5	54.6	55.6	56.5	57.4
50	49.0	50.3	51.6	52.9	54.1	55.2	56.3	57.2	58.1
55	49.7	51.0	52.3	53.6	54.8	55.9	57.0	58.0	58.9
9:00	50.4	51.7	53.0	54.3	55.5	56.5	57.7	58.7	59.6
05	51.1	52.4	53.7	55.0	56.2	57.3	58.4	59.5	60.4
10	51.8	53.1	54.4	55.7	56.9	58.0	59.1	60.2	61.2
15	52.5	53.8	55.1	56.4	57.7	58.8	59.9	61.0	61.9

TABLE 1—(Continued)

P-O (min.: sec.)	Focal depth in km.								
	25	100	200	300	400	500	600	700	800
9:20	53.2	54.5	55.8	57.1	58.4	59.6	60.7	61.8	62.7
25	53.9	55.2	56.6	57.9	59.1	60.3	61.5	62.6	63.5
30	54.6	55.9	57.3	58.6	59.9	61.1	62.3	63.4	64.3
35	55.3	56.6	58.0	59.3	60.6	61.9	63.1	64.2	65.1
40	56.0	57.3	58.7	60.0	61.3	62.6	63.9	65.0	65.9
45	56.7	57.9	59.4	60.8	62.1	63.4	64.7	65.8	66.7
50	57.3	58.6	60.1	61.5	62.9	64.3	65.5	66.6	67.5
55	57.9	59.3	60.8	62.3	63.7	65.1	66.3	67.4	68.3
10:00	58.6	60.0	61.6	63.1	64.6	65.8	67.1	68.2	69.1
05	59.3	60.7	62.4	63.9	65.3	66.6	67.9	69.0	70.0
10	60.0	61.4	63.1	64.7	66.1	67.4	68.7	69.8	70.9
15	60.7	62.2	63.9	65.5	66.9	68.2	69.5	70.7	71.9
20	61.4	62.9	64.6	66.3	67.8	69.0	70.3	71.6	72.8
25	62.1	63.6	65.4	67.1	68.6	69.9	71.2	72.5	73.8
30	62.9	64.3	66.1	67.8	69.4	70.8	72.1	73.4	74.8
35	63.7	65.0	66.9	68.6	70.2	71.7	73.0	74.3	75.7
40	64.4	65.8	67.7	69.4	71.1	72.6	73.9	75.3	76.7
45	65.2	66.5	68.4	70.2	72.0	73.5	74.8	76.2	77.6
50	66.0	67.3	69.2	71.0	72.8	74.4	75.8	77.2	78.6
55	66.7	68.1	70.0	71.9	73.7	75.3	76.7	78.1	79.5
11:00	67.5	68.9	70.9	72.8	74.6	76.2	77.6	79.0	80.4
05	68.3	69.7	71.7	73.7	75.5	77.1	78.6	80.0	81.4
10	69.1	70.5	72.6	74.6	76.5	78.1	79.6	81.0	82.4
15	70.0	71.4	73.5	75.5	77.4	79.0	80.5	82.0	83.5
20	70.8	72.2	74.4	76.4	78.3	80.0	81.5	83.0	84.5
25	71.7	73.1	75.2	77.2	79.1	80.9	82.5	84.0	85.6
30	72.6	74.0	76.1	78.1	80.0	81.9	83.5	85.1	86.7
35	73.5	74.9	77.0	79.0	81.0	82.8	84.5	86.1	87.8
40	74.4	75.8	77.9	79.9	81.9	83.8	85.5	87.2	88.9
45	75.2	76.7	78.8	80.9	82.9	84.7	86.5	88.3	90.1
50	76.1	77.6	79.8	81.9	83.9	85.7	87.6	89.4	91.3
55	77.0	78.5	80.7	82.8	84.8	86.7	88.6	90.5	92.4
12:00	77.8	79.4	81.6	83.8	85.8	87.8	89.7	91.5	93.5
05	78.7	80.3	82.6	84.8	86.9	88.8	90.8	92.7	94.7
10	79.6	81.2	83.6	85.9	87.9	89.9	91.9	93.9	95.8
15	80.6	82.2	84.6	86.9	89.0	91.1	93.1	95.0	96.9

TABLE 1—(Concluded)

P-O (min.: sec.)	Focal depth in km.								
	25	100	200	300	400	500	600	700	800
12:20	81.6	83.2	85.6	87.9	90.1	92.2	94.2	96.1	98.0
25	82.6	84.2	86.6	89.0	91.2	93.3	95.3	97.3	99.2
30	83.6	85.2	87.6	90.0	92.3	94.5	96.5	98.4	100.3
35	84.6	86.2	88.7	91.1	93.4	95.6	97.6	99.6	101.5
40	85.6	87.2	89.8	92.2	94.5	96.7	98.7	100.7	102.6
45	86.6	88.2	90.9	93.3	95.6	97.8	99.8	101.8	103.7
50	87.6	89.3	92.0	94.5	96.8	99.0	101.0	103.0	104.8
55	88.6	90.5	93.1	95.6	97.9	100.1	102.1	104.1	105.9
13:00	89.7	91.6	94.2	96.7	99.0	101.2	103.3	105.2	107.1
05	90.8	92.7	95.3	97.8	100.1	102.3	104.4	106.3	108.2
10	91.9	93.9	96.5	98.9	101.2	103.5	105.5	107.5	109.3
15	93.0	95.0	97.6	100.0	102.4	104.6	106.7	108.6	110.4
20	94.1	96.1	98.7	101.1	103.5	105.7	107.8	109.7	111.5
25	95.2	97.3	99.9	102.3	104.7	106.9	108.9	110.8	112.7
30	96.3	98.4	101.0	103.4	105.8	108.0	110.1		
35	97.5	99.5	102.1	104.6	106.9	109.1	111.2		
40	98.6	100.6	103.3	105.7	108.0	110.3			
45	99.7	101.7	104.4	106.8	109.2	111.5			
50	100.8	102.9	105.5	108.0	110.4				
55	101.9	104.0	106.6	109.1	111.5				
14:00	103.0	105.1	107.8	110.3					
05	104.1	106.2	108.9	111.5					
10	105.2	107.4	110.0						
15	106.1	108.5	111.1						
20	107.5	109.6	112.3						
25	108.6	110.7							
30	109.7								

TABLE 2
CHARACTERISTIC INTERVALS (MIN.:SEC.) OF S-P (UPPER SECTIONS OF TABLE) AND DIFFERENCES OF P FOR PAIRS OF STATIONS IN DEEP-
FOCUS EARTHQUAKES (LOWER SECTIONS OF TABLE)

(a) South American shocks										
Year Day Hour:minute	1920 May 25 11:59.6	1935 Dec. 14 1:31.2	1930 Aug. 4 5:04.5	1933 Aug. 29 14:52.6	1932 Dec. 9 8:34.9	1934 June 24 5:59.6	1933 Oct. 25 23:28.3	1936 Jan. 14 14:12.2	1934 Mar. 1 21:45.4	
Latitude	8½ S	9½ S	9½ S	11 S	15 S	22 S	23 S	29 S	40 S	
Longitude	75½ W	70½ W	70½ W	69½ W	75 W	68½ W	66¾ W	62½ W	72½ W	
Depth in km.	150	650	650	650	70	100	220	620	120	
Station—										
La Plata	4:52	4:09		3:42	3:28	2:40	2:22	1:29	2:23	
Sucre	2:36	2:02					0:45	2:00	3:50	
La Paz	1:54	1:38	1:34	1:27	1:14	1:18	1:22	2:09	4:09	
Huancayo		1:12		1:17		2:15	2:26	2:20	4:38	
San Juan		3:57		4:10	5:22	6:02	5:53		7:50	
Capetown		9:26					8:53	8:10	9:00	
Wellington						11:06	10:51		9:40	
St. Louis	6:47	6:25	6:28	6:41	7:40	8:30	8:26	8:31	9:55	
Fordham			6:24	6:35	7:40	8:27	8:22		10:00	
Ottawa	7:18	6:52					8:48		10:23	
Pasadena	7:55	7:40	7:41	7:47	8:34	9:22	9:25	9:21	10:32	
San Fernando		8:55				10:13	9:56	9:27		
Cartuja	9:45	9:04	9:02	8:58		10:16		9:28		
Zürich			9:55			10:29	11:06			

Santiago-Huancayo	3:34	2:35		3:18	-0:12	-0:54	-1:13	-4:07
La Plata-La Paz		0:31	3:03	3:37	1:50	-1:17		-2:10
San Juan-La Plata		3:06	0:31	1:24	4:04	4:26		6:47
San Juan-La Paz			3:34	5:01	5:54	5:43		4:37
Wellington-Pasadena					1:35	1:36		-0:34
Christchurch-Pasadena					1:37		0:47	-0:38
Pasadena-Fordham			1:21	0:58	1:04	1:07		0:23
Pasadena-Ottawa	0:20	0:51			0:34	0:38		-0:01
San Fernando-Pasadena		1:23			0:54	0:40	0:09	1:06
Cartuja-Victoria		0:17	-0:18		-0:02			
Strasbourg-Pasadena	3:24	2:25				1:46		
Neuchâtel-Pasadena			2:19		1:56	1:43	1:14	
Pasadena-La Plata	3:23	4:54	4:48	5:13	7:58	8:20	9:33	9:26
Hong Kong-Pasadena			10:09		7:41	7:54	7:46	
Chiufeng-Pasadena		9:09	9:03		8:27	7:16	7:42	7:28
Manila-Pasadena		9:32	9:32	9:32	8:31	7:32	7:41	7:10

TABLE 2—(Continued)
(b) Tonga-Fiji region

Year. Day Hour: minute	1935 Jan. 1 13:21.0	1935 July 15 14:13.6	1935 July 29 7:38.9	1933 Sept. 6 22:08.5	1934 Oct. 10 15:42.1	1934 Dec. 15 19:14.4	1932 May 26 16:09.7	1931 Oct. 18 4:30.5
Latitude	17½ S	19½ S	20¼ S	21½ S	23½ S	23½ S	25½ S	26 S
Longitude	174½ W	178½ W	178 W	179¾ W	180	179½ W	179¼ E	180
Depth in km..	300	580	510	600	540	530	600	500
<i>Station—</i>								
Wellington.....	4:06		3:17	2:48		2:59		2:27
Christchurch.....	4:36		3:28		3:15	3:16		3:01
Riverview.....	5:11	4:14	4:21	4:09		4:03	4:02	3:55
Amboina.....		6:56	7:03	6:59		6:58	6:55	6:36
Manila.....	8:54		8:30	8:19	8:24	8:30	8:25	
Batavia.....	9:26	8:40	8:53	8:37	8:40	8:40	8:32	8:41
Kobe.....	8:22	8:33	8:45	8:31	8:37	8:40		8:57
Mizusawa.....	8:57		8:27	8:30	8:37	8:43	8:48	8:59
Nagoya.....			8:37	8:42	8:33	8:40	8:47	
Hong Kong.....	9:33	9:11	9:21	9:09	9:10	9:14	9:19	9:24
Chiufeng.....	9:53	9:29	9:40	9:25	9:35	9:35		
Pasadena.....	9:09	9:19	9:29	9:17	9:32	9:36	9:59	9:36
Berkeley.....	9:02		9:16	9:17	9:31	9:31	9:40	9:42
Tucson.....			9:39	9:42	9:57	9:42		9:36

Wellington-Apia.....	4:17	1:53	1:27	0:52	1:00	0:24	0:15
Riverview-Christchurch.....	0:55	1:01		1:02		1:02	1:14
Riverview-Apia.....	5:30	3:16	2:45	2:20		1:50	1:53
Manila-Kobe.....	0:07	-0:03	-0:13	-0:17	-0:16		
Manila-Wellington.....	5:28	6:16	6:13	6:37	6:33	6:50	
Nanking-Riverview.....	5:08	5:52	5:58	6:07	6:13		
Pasadena-Manila.....	0:16	0:52	1:06	1:14	1:10	1:20	
Chiufeng-Pasadena.....	1:06	0:35	0:28	0:22	0:24	0:20	0:23
Pasadena-Wellington.....	5:44	7:08	7:19	7:51	7:43	8:10	8:21
Honolulu-Riverview.....	0:47	2:19	2:35	3:07		3:29	
Pasadena-Hong Kong.....		-0:01	0:14	0:17	0:17	0:25	0:25
Hamburg-Pasadena.....		7:33	7:22	7:17	7:19	7:13	7:13
Kew-Pasadena.....	8:00	7:36	7:25	7:21			7:18
Strasbourg-Pasadena.....	8:07	7:37	7:29	7:23		7:19	7:20
Zürich-Pasadena.....	8:09	7:44	7:30			7:20	7:24

Wellington-Manila.....	-5:47	-3:40	-3:57	-0:15	-0:20	4:08	4:41	4:45
Christchurch-Chiufeng.....	-7:10		-5:33		-2:10			
Wellington-Batavia.....		-4:02	-4:32	-1:23	-1:20	4:17	5:29	
Phu Lien-Christchurch.....	6:49			2:08	1:34			-7:52
Chiufeng-Riverview.....	7:17		6:13	4:14	4:00	2:06	1:16	
Nanking-Adelaide.....			3:32				1:06	-3:10
Bombay-Chiufeng.....			2:16			1:35	1:03	
Honolulu-Manila.....	-1:16	0:05	-0:38	1:41				
Mizusawa-Melbourne.....	5:07	3:44	3:55	1:52	1:52	1:54	1:36	
Helwan-Pasadena.....	6:44		6:38			-0:59	-1:39	-7:54
Pasadena-Chiufeng.....	0:40		1:13		3:07		6:18	11:17
Pasadena-Hong Kong.....	1:33		2:02	4:08	4:15	8:11	8:34	13:33
Copenhagen-Pasadena.....	6:42			7:39	5:48	-0:36	-0:43	-6:20
Strasbourg-Pasadena.....	6:57		6:47	6:09	6:02	3:55	-0:22	-6:04
La Paz-Strasbourg.....		-0:15	-0:44	0:03	-0:02	1:10	5:09	-7:15

TABLE 2—(Continued)
(d) Philippine Islands, Marianne Islands, South of Japan

Year Day Hour:minute	1926 Oct. 30 13:46.6	1929 Apr. 8 10:16.9	1929 June 4 15:16.0	1931 Sept. 9 20:38.5	1933 Sept. 2 16:41.1	1932 Apr. 4 19:16.5	1928 Mar. 29 5:06.0
Longitude	123° E	124½° E	124½° E	145½° E	138½° E	138½° E	138½° E
Latitude	9½° N	7¾° N	6¼° N	19¼° N	20° N	20° N	31¾° N
Depth in km.	520	610	380	180	410	410	410
<i>Station—</i>							
Manila.....		1:33	1:43	4:34	3:46	3:21	3:39
Hong Kong.....	1:52	2:47		4:44	3:44	3:42	3:43
Zikawei.....	3:23		3:55	4:24		2:27	2:00
Chiufeng.....					3:28	3:10	
Kobe.....		4:10	4:32		1:10		0:57
Nagoya.....		4:19		3:07	1:06	1:05	0:51
Mizusawa.....	4:56	4:28	5:03	3:41	1:40	1:37	1:27
Phu Lien.....			3:31	5:23	4:32		4:30
Batavia.....		3:26	3:27	6:27	6:22	6:21	6:24
Bombay.....		6:29	6:47	8:44			7:30
Riverview.....		6:21	6:20	7:16	8:06		
Adelaide.....		5:56		7:09	8:11		8:17
Melbourne.....		6:27		7:02	8:45		
Honolulu.....				6:40	7:26	7:30	7:22
Pasadena.....				10:04	9:40	9:45	9:44
Ksara.....		9:34				9:41	9:35
Tashkent.....		7:20	7:42	8:40	7:12	7:12	7:07
Kew.....					10:17		10:09

Manila-Hong Kong.....	-1:38	-1:35	-1:48	-0:48	-0:07	-0:06	-0:02
Chiufeng-Manila.....					-0:13	-0:19	
Phu Lien-Hong Kong.....		0:36	0:38	1:02	1:04		1:01
Batavia-Mizusawa.....		-1:51	-2:05	3:45	5:48	5:51	6:12
Bombay-Zikawei.....		3:45	3:48	5:40			6:23
Adelaide-Honolulu.....				0:02	1:48		1:43
Pasadena-Manila.....				7:12	7:14	7:14	7:14
Pasadena-Chiufeng.....					7:27	7:33	
Pasadena-Strasbourg.....				-1:23	-0:33	-0:33	-0:23
Pasadena-Nagoya.....				8:18	10:13	10:16	10:31
Pasadena-Ksara.....						-0:01	0:05
La Paz-Pasadena.....				7:10	7:24	7:23	

TABLE 2—(Concluded)
(e) Region of Japan, eastern Siberia, and Kamchatka

Year.....	1931	1929	1931	1930	1929	1930	1930	1934
Day.....	June 29	June 2	Feb. 20	Jan. 5	Jan. 13	Mar. 10	Jan. 3	Jan. 3
Hour:minute	16:43.2	21:38.5	5:33.4	1:19.8	0:03.2	16:27.4	9:42.4	9:42.4
Longitude.....	136° E	137° E	135½ E	154 E	154½ E	149 E	156½ E	156½ E
Latitude.....	34 N	34½ N	44½ N	49 N	49½ N	50 N	52½ N	52½ N
Depth in km.....	360	360	350	140	140	620	280	280
<i>Station—</i>								
Manila.....	4:03		4:52	6:21		5:30	6:34	
Hong Kong.....		3:48	4:18	6:07	6:01	5:09	6:11	
Zikawei.....	2:22	2:20	3:04	4:52		4:00	4:56	
Chiufeng.....	3:06		2:41				4:36	
Kobe.....	0:38	0:40	1:46	3:41	3:53	2:54	3:52	
Nagoya.....	0:39	0:36	1:44	3:30	3:36		3:46	
Mizusawa.....	1:08	1:09		2:30	2:53	2:11	3:05	
Phu Lien.....		4:32		6:38	6:49	6:00		
Batavia.....		6:35	7:25	8:51	8:57		9:00	
Bombay.....		7:35	7:28	8:59	9:00	7:55	8:53	
Riverview.....		8:32	9:31	10:12	10:06		10:13	
Adelaide.....		8:37	9:31		10:03		10:23	
Melbourne.....			9:48		10:32			
Wellington.....		9:43			10:56			
Honolulu.....		5:35			6:50		6:33	
Pasadena.....	9:46	9:44	9:18	8:22	8:23	8:04	7:56	
Sitka.....				9:21	6:02		5:32	
Ottawa.....				9:55	9:22			
Ksara.....		9:33	8:55		9:53	8:58	9:51	

Tashkent.....	7:01	6:28	9:31	9:23	6:45	9:06
Uccle.....		9:14		9:39	8:48	9:17
Strasbourg.....		9:20			8:52	
Manila-Hong Kong.....	0:09	0:42	0:28	0:19	0:31	0:29
Chiufeng-Manila.....	1:03		0:49	0:41	0:30	-2:25
Phu Lien-Hong Kong.....	6:42	7:23	7:44	7:42		7:22
Batavia-Mizusawa.....						
Bombay-Zikawei.....						
Pasadena-Manila.....	6:22	5:37	4:56	4:48	4:46	4:36
Pasadena-Chiufeng.....	6:59	5:15	2:13	2:08	2:53	1:35
						4:00
Pasadena-Strasbourg.....	-0:19	0:05	-1:25	-1:30	-0:51	-1:23
Sitka-Honolulu.....				-0:54		-1:15
Pasadena-Nagoya.....	10:55	9:06	5:58	5:47		5:20
Pasadena-Ksara.....	0:11	0:21	-1:44	-1:45	-1:00	-1:48
Fordham-Pasadena.....		1:08		1:44		1:35
St. Louis-Pasadena.....	1:02	0:53	1:14	1:12	1:01	1:09
Victoria-Manila.....	6:08			0:43		-0:02
Ottawa-Pasadena.....		0:50	1:20	1:17		1:09
La Paz-Pasadena.....	7:25	7:38	8:48	8:52	8:23	8:56

TABLE 3

DISTANCES Δ FOR SHOCKS IN THE FIJI REGION(A: 1931, Oct. 18; B: 1932, May 26; C: 1934, Dec. 15; D: 1933, Sept. 6; E: 1931, April 3; F: aftershock of B, 1932, May 26, 22^h 21^m9.)

Station	Azimuth		Δ from P-O and H					Differences in Δ				
	A	E	A	B	C	D	E	^(a) B-A	^(b) B-F	^(c) B-C	^(d) B-D	^(e) E-D
Apia.....	39	57	14.5	13.6		11.1		-0.9	-0.5		2.5	
Wellington.....	195	190	15.9	15.7	18.7	19.8	21.6	-0.2	0.2	-3.0	-4.1	1.8
Christchurch.....	197		18.6	18.3	22.3			-0.3	0.1	-4.0		
Riverview.....	244	234	26.4	25.2	27.3	28.7	29.3	-1.2	1.0	-2.1	-3.5	0.6
Melbourne.....	239	231	32.2	31.3		34.8	35.6	-0.9			-3.5	0.8
Adelaide.....	244	239	37.0	36.4		39.3	39.3	-0.6			-2.9	0.0
Honolulu.....		30		51.2		47.8	47.6				3.4	-0.2
Anboina.....		280		52.1	53.6				0.7	-1.5		
Perth.....	248	244	56.2	56.3		68.5	67.4	0.1		-1.2	-0.1	-1.1
Manila.....	296		68.4		69.6	72.3	71.6	-0.2	0.0	-2.5	-2.5	-0.7
Batavia.....	273	271	70.0	69.8	72.3	72.3	68.6		-1.3			
Sumoto.....	322	322	74.1		71.7							
Sendai.....	329		74.1			70.7	69.0					-1.7
Kobe.....	322	322	74.1		72.5	70.8	69.4	-2.3		0.0	1.7	-1.4
Mizusawa.....	330	330	74.8	72.5	72.5	77.8	76.5	-1.2		-1.0	0.4	-1.3
Hong Kong.....	300		79.4	78.2	79.2							
Berkeley.....	41	43	83.6	83.1	82.0	80.1	80.1	-0.5	0.0	1.1	3.0	0.0
Pasadena.....	47	48	84.2	83.1	82.6	80.5	80.3	-1.1	-0.8	0.5	2.6	-0.2
Tinemaha.....	44	46	86.1	85.3	84.1	82.3	81.9	-0.8	-0.4	1.2	4.0	-0.4
Phu Lien.....	296		85.7			83.7						
Tucson.....		52		88.0	86.7	85.3	85.7		-0.2	1.3	2.7	0.4
Chufeng.....	317	317	88.8	87.2	87.3	86.1	84.4	-1.6		-0.1	1.1	-1.7
Florissant.....	54			106.0		103.1	104.1				2.9	1.0
La Paz.....	114	114	100.5	100.8		104.6		0.3			-3.8	
Irkutsk.....	323	324	102.1	100.3			101.0	-1.8				

LOCATION OF EPICENTERS

In the previous paper the methods for determining epicenters for deep shocks were largely independent of precise travel times, such as were given in the accompanying tables, the only important assumption being that of identical wave propagation in all azimuths. Such procedure is necessary to establish the travel times, and in part it is required for their revision. However, since the tabulated times of P agree very well with observation, the error for most distances and focal depths probably not exceeding two seconds, it is possible to assume these times as a basis, either for the revision of travel times of other phases or for the determination of epicenters.

A preliminary determination of the general location of the epicenter is facilitated by comparison with the data of shocks already investigated. Table 2 has been constructed for this purpose. The epicenters and depths given for these shocks are taken from a paper soon to be published.⁴ The table is divided into regional sections, giving for the various shocks the observed S-P intervals at selected stations, and the time differences between the arrivals of P at selected pairs of stations. The stations used have been selected for their location with respect to the epicenters, the reliability of their reported times, or the early date of publication of their bulletins, or for a combination of these reasons. Data for recent and well-observed shocks have been preferred. The intervals given as S-P are as reported by the stations, even where it is probable that the observed phase is SKS. In the second section the first recorded phase has been used in each case, irrespective of whether it proves to be P or P'.

As an example of this procedure we may take the shock of January 5, 1937, at 11^h. The readings at Pasadena are:

iP.	11	20	51
epP.	22	36	
iS.	30	32	
iSKPP'.	49	35	

These data give a distance of 85° and a depth of 470 km., with origin time 11:09.1. For the methods used, refer to the previous paper. At the time when the Pasadena bulletin was being prepared, we had already received data for the following stations, either directly or by way of Strasbourg:

				S-P
Nanking.	P 12:54	S 15:49		2:55
Manila.	P 13:23	S? 15:30		—
Chiufeng.	P 13:30	i 15:47	S 16:45	3:15
Hong Kong.	P? 13:38	S? 16:06	SS? 17:10	3:32
Phu Lien.	iP 14:45	iS 19:08		4:23

⁴ B. Gutenberg and C. F. Richter, "Depth and Geographical Distribution of Deep-Focus Earthquakes," a paper presented at the joint meeting of the Geological Society of America, Cordilleran Section, and the Seismological Society of America, at Berkeley, April 10, 1937.

The S—P intervals are tabulated as identified by comparison with the origin time determined at Pasadena. Since Nanking is the nearest station, with a travel time for P of 3.8 minutes, an origin in the Japanese region is suggested; the other stations confirm this with the foregoing interpretation of the readings. We now compare with sections (d) and (e) of table 2. Using the values of S—P for Chiufeng, Hong Kong, Phu Lien, and Pasadena (9^m 41^s), we find reasonable agreement with the last three columns under (d) and the first two under (e). To discriminate more closely we may make use of the time differences between P at pairs of stations. The best agreement is with the shock of September 2, 1933. We here tabulate the differences in the two cases for direct comparison:

	1937, Jan. 5	1933, Sept. 2
Manila-Hong Kong.	-0:15	-0:07
Chiufeng-Manila.	0:07	-0:13
Phu Lien-Hong Kong.	1:07	1:04
Pasadena-Manila.	7:18	7:14
Pasadena-Chiufeng.	7:21	7:27

The differences Pasadena-Chiufeng and Chiufeng-Manila are definitely out of agreement with the data of the shocks in section (e).

Using all the data, the epicenter is found to be approximately 28° N, 138° E.

When the data of a considerable number of stations are available, such a comparison of shocks can be used for a precise determination of the relative positions of the epicenters. This requires that the origin times and depths be first determined to a good approximation, by the methods outlined in the previous paper. For any one station the distances corresponding to the travel times of P for two given shocks can be read off from table 1. The differences between these calculated distances can then be plotted as a function of the azimuth of the stations. No great precision is required in the azimuth, which can usually be taken with sufficient accuracy from one of the shocks in the same region tabulated in the International Summary.

Examples of the calculated difference in distance for a group of shocks in the Fiji-Tonga region are given in table 3. For shocks A, D, and E the values of P—O are given in table 4. The differences given in table 3 are plotted as functions of azimuth in figure 2.

The figure shows clearly that the calculated differences can be represented closely by properly drawn sine curves, as is to be expected. The equation of such a curve may be written $y - c = A \cos (x - a)$.

Here A , the amplitude of the sine function, is the distance between the two epicenters. The azimuth $x = a$ gives the maximum of y , and this determines the direction of the line joining the two epicenters. The constant c indicates that the curve is not symmetrical with respect to the zero line; this may be due either to a slightly incorrect origin time or to a slight error in the assumed focal depth, in one or both shocks. The correspondence between the effect of error in

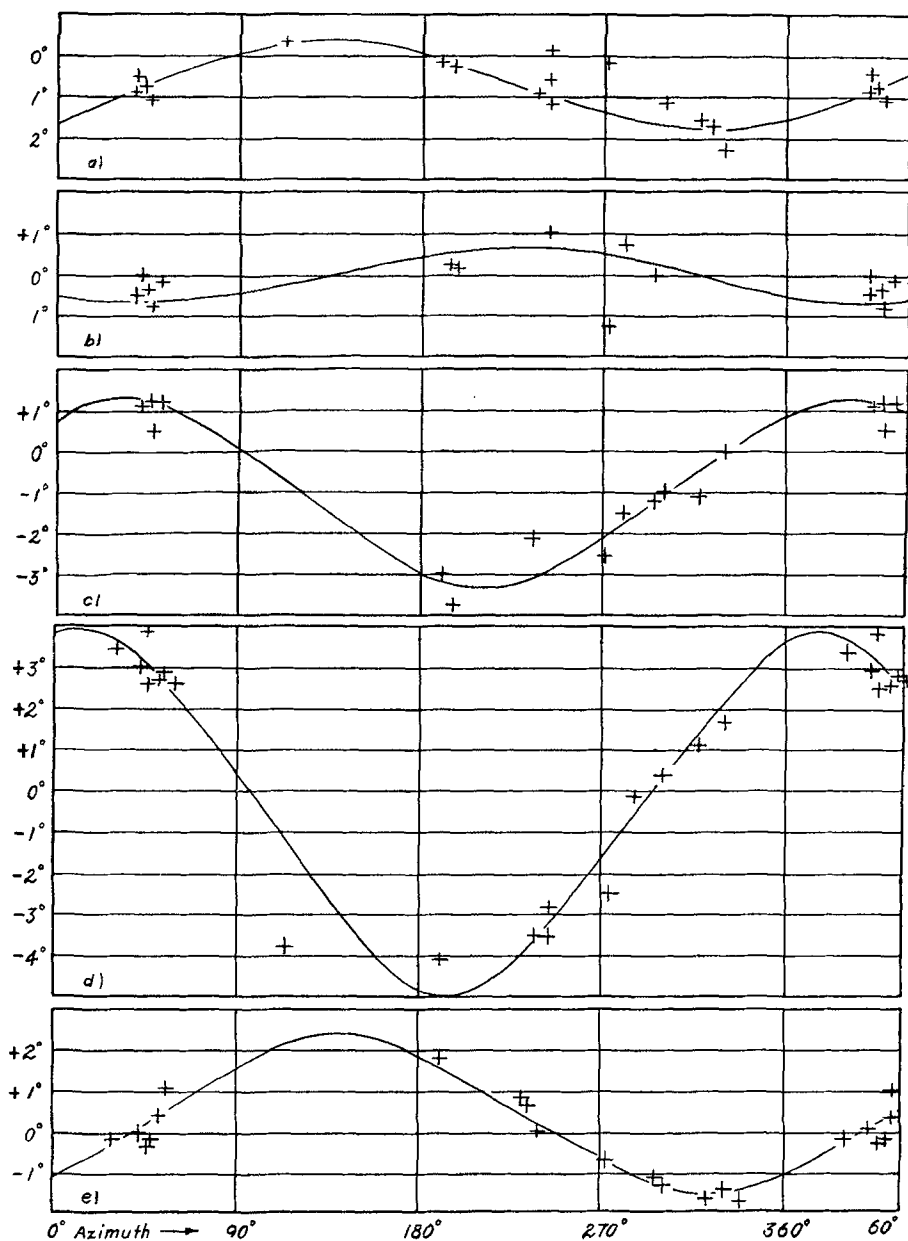


Fig. 2. Differences in epicentral distances for a group of shocks in the Fiji-Tonga region (see table 3), plotted as functions of azimuth.

origin and error in depth is exhibited in the following tabulation. If the assumed origin time is one second too late, then the calculated distances are too small by the amounts shown :

Distance (deg.)	Focal depth		
	100 km.	400 km.	700 km.
10.....	.07	.08	.12
30.....	.12	.12	.12
60.....	.14	.15	.15
90.....	.23	.23	.23

If the assumed depth is 10 km. too large, then the calculated distances are too large by the amounts shown :

Distance (deg.)	Focal depth		
	100 km.	400 km.	700 km.
10.....	+.01	.00	-.02
30.....	.12	+.10	+.04
60.....	.16	.12	.09
90.....	.26	.22	.19

If there is an error in the assumed depth or origin time, and most of the stations are at about the same distance, the result will be a vertical displacement of the curve drawn to represent the distance residuals. If there are available stations distributed over a considerable range of distance in about the same azimuth, the plotted residuals will show an effect of distance, directly suggesting a revision in depth or origin time. However, as the preceding tabulations show, except when there are a number of good stations at very short distances, it may not be possible to decide from these residuals alone whether the correction should be applied to the depth or to the origin time, or to both. In fact, if the assumed origin time is E seconds too late, and the assumed depth is also $10E$ kilometers too large, the two errors will very nearly compensate for all except the shortest distances. Thus a good agreement among the data does not necessarily mean that the depth and origin time are both correct. On the other hand, if the residuals show a large scatter about the mean sine curve, the error is more likely to be in the depth than in the origin time.

In most of these cases it will be observed that the location of the epicenter is not likely to be much affected, provided that the available stations are reasonably numerous and well distributed in azimuth.

By making use of the other principal recorded phases it appears possible to separate error in depth from error in origin time; this point requires further discussion, which is reserved for a later paper.

We may proceed to draw a few specific conclusions from the curves of figure 2. In the curve *a*) we have $A=1^\circ$ and $a=140^\circ$, approximately; consequently shock B is about 1° northwest of shock A. (For dates of shocks refer to table 3.)

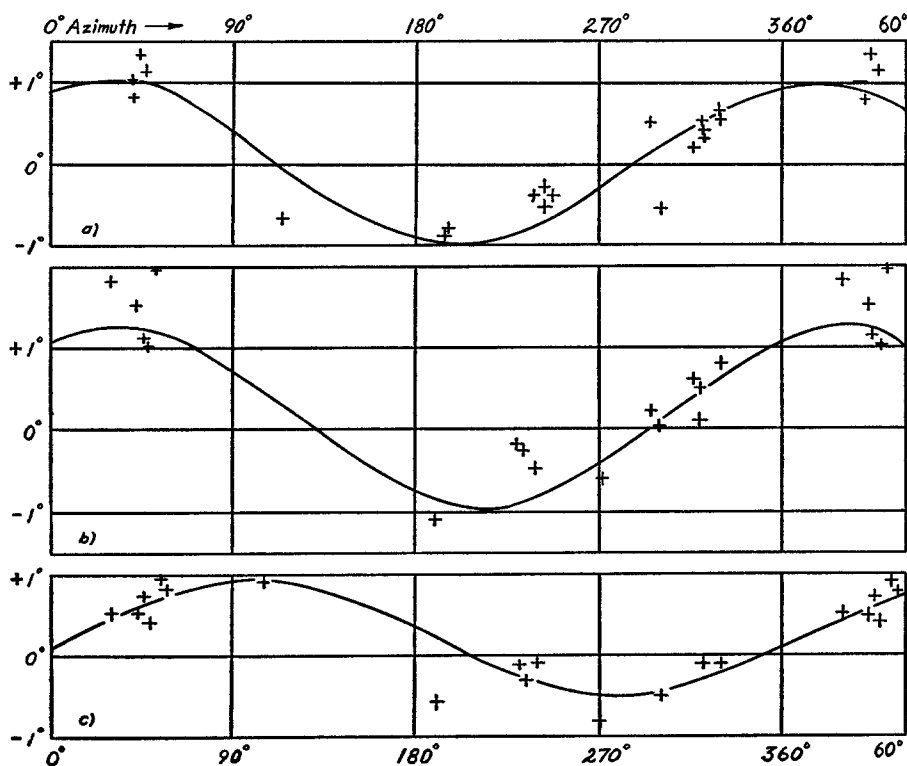


Fig. 3. Differences in epicentral distances, $\Delta_1 - \Delta_2$, plotted from table 4 as functions of azimuth.

We have $c = -\frac{1}{2}^\circ$; this is probably due to a combination of small errors in the depths and origin times of the two shocks. The curve *b*) shows that the strongest aftershock of the large earthquake B originated within less than a degree from the main shock. The remaining three curves show that shock B originated about $2\frac{1}{2}^\circ$ south and somewhat west of C, and $4\frac{1}{2}^\circ$ south and slightly west of D, and that shock E originated about 2° northwest of D.

When no shock is available for comparison, or when it is desired to fix the absolute geographical position of the epicenter, a similar method can be used. As before, the depth and origin time are determined as precisely as possible,

and the distances are determined from these by using table 1. These distances are then compared with distances calculated from an assumed approximate epicenter, and the residuals are plotted as functions of the azimuth. Table 4 and figure 3 give three examples of this procedure. For shocks *a*) and *b*) the epicenters given in the International Summary were taken as first approximations. For shock *c*) the distances were calculated from the adopted epicenter, using geocentric latitudes. The plotted curves indicate that shocks *a*) and *b*) are about 1° south of the International Summary epicenters, and that shock *c*) occurred about 1° west of the adopted epicenter.

By combining both methods, and using epicenters located carefully by the method of least squares, as in the previous paper, an entire group of epicenters can be located with precision, both absolutely and relatively. The epicenters given in table 2 have been corrected by these methods, and are the best we can give at present for these particular shocks.

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